### PHP2530: Bayesian Statistical Methods Fall 2013

Mon, Wed 9:00 – 10:20 121 South Main St. Rm 241

#### **Instructor Information**

Roee Gutman 121 South Main St. Rm 721

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#### **Office Hours**

Mon, Wed 10:30-11:30 pm and by appointment

#### **Recommended Text**

Gelman, A., Carlin, J.B., Stern, H.S., and Rubin, D.B. (2004). *Bayesian Data Analysis* (2<sup>nd</sup> Edition). Chapman and Hall/CRC.

### **Objectives**

The Bayesian approach to statistics differs in a number of ways from the classical or "frequentist" approach, including the ability for Bayesians to flexibly incorporate prior knowledge/experience in data analyses. Modern advances in computing have allowed many complicated models, which are difficult to analyze using conventional frequentist methods, to be straightforwardly analyzed using Bayesian methodology. The Bayesian paradigm for data analysis can be described as consisting of four main steps: constructing probability models for data given parameters, computing posterior distributions of parameters, exploring posterior distributions, and checking/improving models. This course exposes students to the Bayesian approach and its conceptual underpinnings. Basic Bayesian models are introduced at the beginning, and then more complicated hierarchical and mixture models are described, many of which have important applications in a variety of fields.

### **Prerequisites**

Some prior exposure to statistical inference will be extremely useful for this class. If you are concerned that you do not have a sufficient background for this class, please see the instructor.

#### **Computational Requirements**

The free BUGS (Bayesian inference Using Gibbs Sampling) software and R software will be used in assignments and classes for fitting Bayesian models. In addition, students will be required to write their own code (such as simulations, sampling, Markov Chain Monte Carlo) in one other programming language of their choice (R, Matlab, Fortran, C++, etc.). Students who do not have

prior experience with such programming languages are strongly encouraged to gain some working knowledge of one early in the semester, independent of the class. Computational proficiency is essential for modern Bayesian analysis and will be stressed during the course.

## Course requirements and grades

- Class participation (10%)
- Homework (40%) there will be 5-6 homework assignments.
- Final project and presentation (50%). The final project will be either an application of material learned in the course to a problem or a dataset, or a methodological investigation/improvement of existing methods.

### **Course Outline**

### **PART I: Fundamentals of Bayesian Inference (4 weeks)**

- Week 1: Introduction, the Bayesian paradigm
- Week 2: Perspectives on probability, univariate and multi-parameter models
- Week 3: Likelihood Principle, prior selection, decision theory
- Week 4: Exchangeability, hierarchical models, Bayesian inference

# PART II: Bayesian Computation & Modeling (5 weeks)

- Week 5: Quadrature, importance sampling
- Week 6: Model selection, hypothesis testing, Bayes factor
- Week 7: EM and its extensions
- Week 8: Gibbs sampling, MCMC
- Week 9: MCMC continued and diagnostics

## **PART III: Applications of Bayesian Inference (5 weeks)**

- Week 10: Regression models, data collection, randomization, ignorability
- Week 11: Causal inference framework, missing data formulation
- Week 12: Principal stratification & compliance
- Week 13: Spatial data modeling
- Week 14: Meta Analysis and Clinical Trials

## **Additional Bibliography**

- Berger J. (1985) Statistical Decision Theory and Bayesian Analysis (2nd Edition). Springer Verlag
- Box, G.E.P., Tiao, G.C. (1973) Bayesian Inference in Statistical Analysis, Addison-Wesley.
- Albert J. (2007) Bayesian Computation with R. Springer.
- Robert C. and Casella G. (1999) Monte Carlo Statistical Methods. Springer Verlag.
- Gelman A., Hill J. (2007) Data Analysis Using Regression and Multilevel/Hierarchical Models. Cambridge University Press.
- Carlin B, Louis T (2008) Bayes and empirical Bayes methods for data analysis, Chapman & Hall/ CRC.
- Selected articles.