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> restart;
> #preferences single household;
> x0:=(c-2*eta)*(g-eta);

$$x0 := (c - 2\eta)(g - \eta) \quad (1)$$


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> #substitute budget constraint
x1:=subs(g=y-c,x0);

$$x1 := (c - 2\eta)(y - c - \eta) \quad (2)$$


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> #optimal food consumption;
x2:=solve(diff(x1,c),c);


$$x2 := \frac{1}{2}y + \frac{1}{2}\eta \quad (3)$$


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> #foodshare is decreasing in income
x2a:=x2/y;
simplify(diff(x2a,y));


$$\begin{aligned} x2a &:= \frac{\frac{1}{2}y + \frac{1}{2}\eta}{y} \\ &\quad - \frac{1}{2}\frac{\eta}{y^2} \end{aligned} \quad (4)$$


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> #joint household--maximize sum of utilities but combine income
and share public good ;
#delta is cost of joint residence;
x3:=(c1-2*eta)*(2*y-c1-c2-eta)+(c2-2*eta)*(2*y-c1-c2-eta)-delta;

$$x3 := (c1 - 2\eta)(2y - c1 - c2 - \eta) + (c2 - 2\eta)(2y - c1 - c2 - \eta) - \delta \quad (5)$$


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> #focus on total food consumption
> x4:=simplify(subs(c1=c-c2,x3));

$$x4 := -c^2 + 3c\eta + 2cy + 4\eta^2 - 8\eta y - \delta \quad (6)$$


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> #optimal food consumption
x5:=solve(diff(x4,c),c);

$$x5 := \frac{3}{2}\eta + y \quad (7)$$


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> #food share in joint household
> x5a:=x5/(2*y);
simplify(diff(x5a,y));


$$\begin{aligned} x5a &:= \frac{1}{2} \frac{\frac{3}{2}\eta + y}{y} \\ &\quad - \frac{3}{4}\frac{\eta}{y^2} \end{aligned} \quad (8)$$

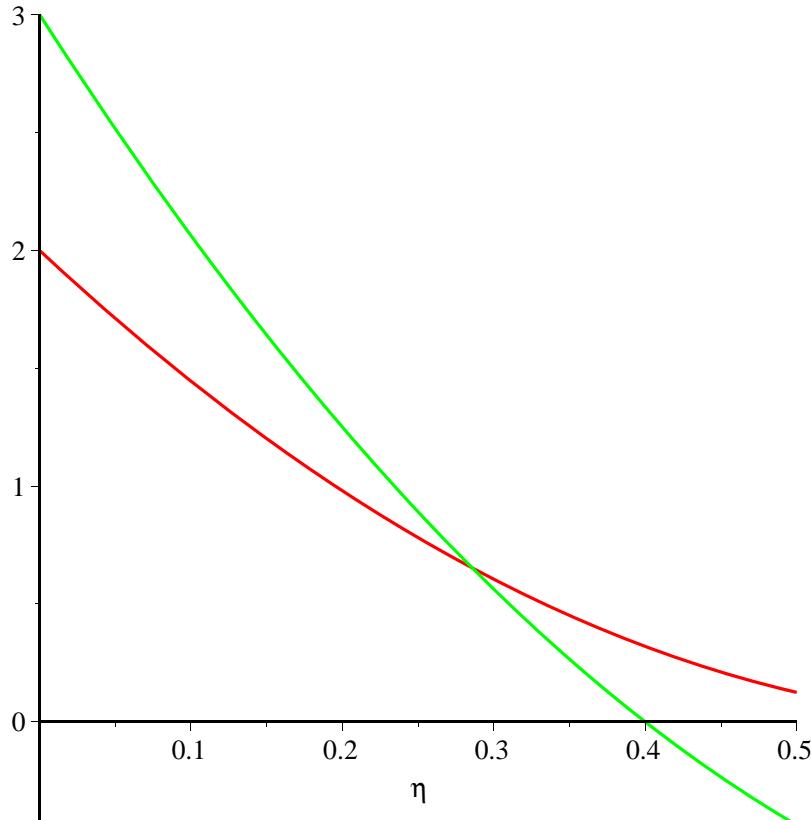

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> #total utility in joint household;
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$$x6 := \text{simplify}(\text{subs}(c=x5, x4)); \\ x6 := \frac{25}{4} \eta^2 - 5 \eta y + y^2 - \delta \quad (9)$$

$$> \#combined utility if in separate households; \\ x7 := 2 * \text{subs}(c=x2, x1); \\ x7 := 2 \left(\frac{1}{2} y - \frac{3}{2} \eta \right)^2 \quad (10)$$

> #joint utility is higher when eta is higher;
 $\text{plot}(\text{subs}(y=2, \text{delta}=1, [x7, x6]), \text{eta}=0..0.5, \text{color}=[\text{red}, \text{green}]);$



$$> x8 := [\text{solve}(\text{subs}(y=2, \text{delta}=1, x6=x7), \text{eta})][2]; \\ x8 := \frac{2}{7} \quad (11)$$

$$\frac{1}{2} \frac{\frac{4}{3} y + \frac{2}{3} \eta}{y} \quad (12)$$

> #foodshare is always higher in split households for given eta.
 #but note that joint households only if eta>.6

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#but split households only if eta<.6
#average foodshare for split households may be lower than joint.
plot(subs(y=2,[x2a,x5a,piecewise(eta>x8,x2a,x5a)]),eta=0..0.5,
color=[red,green,blue]);
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